# Electronic Structure of $Ru_2(O_2CR)_4^+$ and $Rh_2(O_2CR)_4^+$ Complexes

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Abstract: SCF-X $\alpha$ -SW calculations of Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup>, Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub><sup>+</sup>, Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>, Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub><sup>+</sup>, and  $Rh_2(O_2CH)_4^+$  are used to discuss the bonding, magnetic properties, stable oxidation level, axial ligand trans influence, electronic spectra, and ESR spectra of ruthenium and rhodium carboxylate dimers. The Ru(2.5) dimers are predicted to have a  $\sigma^2 \pi^4 \delta^2 \pi^{*2} \delta^{*1}$  configuration, corresponding to three unpaired electrons as found by experiment. For the Rh(2.5) dimers, the predicted configuration is  $\sigma^2 \pi^4 \delta^2 \pi^{*4} \delta^{*1}$ . Reasons for the close spacing of  $\pi^*$  and  $\delta^*$  orbitals, and the energy order  $\pi^* < \delta^*$ , are discussed. Favorable exchange energy and susceptibility of the Ru(II) dimer to Jahn-Teller distortion are seen as factors stabilizing the Ru(2.5) oxidation level. An explanation is given for the observed changes in Rh-Rh, Rh-OH2, and Rh-O(acetate) distances between  $Rh_2(O_2CR)_4(H_2O)_2$  and  $Rh_2(O_2CR)_4(H_2O)_2^+$ . Comparison of  $Ru_2(O_2CH)_4Cl_2^-$  and  $Rh_2(O_2CH)_4-Cl_2^-$  and  $Rh_2(O_2$  $(H_2O)_2^+$  indicates that Cl<sup>-</sup> is slightly better than  $H_2O$  at weakening a trans metal-metal bond. The observed order of Rh-Rh distances in  $Rh_2(O_2CCH_3)_4L_2$ , L = H<sub>2</sub>O, py, NHEt<sub>2</sub>, CO, PR<sub>3</sub>, is interpreted as consistent with the X $\alpha$ -SW energy level diagram. The prominent band near 2  $\mu$ m<sup>-1</sup> in the visible spectrum of Ru<sub>2</sub>(O<sub>2</sub>CR)<sub>4</sub><sup>+</sup> complexes is assigned to an O $\pi \rightarrow \pi^*$  transition, where "O $\pi$ " is a mainly Ru-O orbital, but with significant Ru-Ru  $\pi$  character. The weak band near 1  $\mu$ m<sup>-1</sup> in the aqueous solution spectrum is assigned to mainly the  $\delta \rightarrow \delta^*$  transition. The bands near 1.9 and 2.5  $\mu$ m<sup>-1</sup> in the acidic solution spectrum of Rh<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub><sup>+</sup> are assigned to  $\pi^* \rightarrow \sigma^*$  and  $\pi^* \rightarrow Rh-O \sigma^*$  transitions, respectively, as for the analogous bands of  $Rh_2(O_2CCH_3)_4(H_2O)_2$ . The extra band which appears for the cation near 1.3  $\mu$ m<sup>-1</sup> is tentatively assigned to the  $\delta \rightarrow \delta^*$  transition. Good agreement is obtained between calculated and experimental g values for the Ru(2.5) dimers. Problems in developing a suitable model for calculation of hyperfine coupling constants are discussed.

A significant fraction of our efforts to provide accurate theoretical models for metal-metal bonded compounds<sup>2-7</sup> is directed toward the dinuclear carboxylates  $M_2(O_2CR)_4L_2$ , which have idealized  $D_{4h}$  symmetry when the carboxylate substituents R are planar and the axial ligands L are linear. These have been structurally characterized for a wide variety of metals, namely,  $M = V^{2+}$ ,  $Cr^{2+}$ ,  $Co^{2+}$ ,  $Cu^{2+}$ ,  $Mo^{2+}$ ,  $Tc^{3+}$ ,  $Ru^{2.5+}$ ,  $Rh^{2+,2.5+}$ , and  $Re^{3+.8-16}$  They are thus convenient for studying the variation of metal-metal bonding and metalmetal/metal-ligand bond interactions with M and L for a constant cis ligand framework. We have previously analyzed such questions, and assigned photoelectron and electronic spectra, using SCF-X $\alpha$ -SW calculations of Mo<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>,<sup>3</sup>  $Rh_2(O_2CH)_4$ ,<sup>5</sup> and  $Rh_2(O_2CH)_4(H_2O)_2$ .<sup>5</sup> Others have similarly treated  $Cr_2(O_2CH)_4$ ,<sup>17</sup> and an SCF-HF-LCAO treatment of  $Cr_2(O_2CH)_4$ ,  $Mo_2(O_2CH)_4$ , and  $CrMo(O_2CH)_4$  has recently appeared.<sup>18</sup> The combination of the calculations and sophisticated experimental investigations of structures and spectra<sup>19,20</sup> has greatly increased our understanding of these important compounds.

The Ru<sup>2.5+</sup> carboxylates are well characterized in the solid state as  $[Ru_2(O_2CR)_4]Cl$ , with axial chloride ions bridging two  $Ru_2(O_2CR)_4$  units as depicted in 1,<sup>14a.21</sup> and very recently as



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 $Ru_2(O_2CR)_4Cl_2^-$  and  $Ru_2(O_2CR)_4$  (H<sub>2</sub>O)<sub>2</sub><sup>+</sup>, also depicted in 1.14b The Ru-Ru distances lie between those in  $Mo_2(O_2CCH_3)_4$  (2.09 Å)<sup>13</sup> and  $Rh_2(O_2CCH_3)_4(H_2O)_2$  (2.39 Å), <sup>15a</sup> where our calculations<sup>3,5</sup> indicate quadruple and single metal-metal bonds, respectively. The Ru-Cl bonds are sufficiently weak that the chloro compounds are 1:1 electrolytes in aqueous solution,<sup>21a</sup> reflecting the strong trans influence of the metal-metal bond,<sup>22</sup> which we have discussed in some detail for rhodium(II) carboxylates.<sup>5</sup> These compounds are unique among the strongly metal-metal bonded carboxylate dimers in having the  $M_2(O_2CR)_4$  unit stable as a 1+ ion, so that the average metal oxidation state is nonintegral, and in having three unpaired electrons per dimer.<sup>21a,23</sup> By contrast, their Mo, Tc, Rh, and Re analogues are most stable with neutral or dipositive  $M_2(O_2CR)_4$  units, and are all diamagnetic. Attempts to reduce  $Ru_2(O_2CR)_4^+$  by one electron<sup>21b,23,24</sup> lead only to ill-characterized products or decomposition. A good comparison is with the rhodium system, where  $Rh_2(O_2CCH_3)_4^+$  can be prepared under special conditions<sup>24,25</sup> and indeed even the crystal structure of  $[Rh_2(O_2CCH_3)_4 (H_2O)_2$ ]ClO<sub>4</sub>·H<sub>2</sub>O has been determined, <sup>15c</sup> but the ion easily reverts to the air-stable neutral complex.

These unusual properties have stimulated several experimental investigations of the electronic structure responsible for them. The electronic spectra in aqueous solution (where the species is probably  $Ru_2(O_2CR)_4(H_2O)_2^+$ ) have been reported from the near-infrared to the ultraviolet region,<sup>21a,24</sup> and compared with the spectra of  $Rh_2(O_2CR)_4(H_2O)_2^{0,+}$  and the ephemeral one-electron-reduced Ru compound.24 The diffuse-reflectance spectra of solid  $[Ru_2(O_2CR)_4]Cl$  were described in conjunction with a resonance-Raman study which concluded that the prominent visible absorption near 500 nm is due to a dipole-allowed electronic transition.<sup>26</sup> Frozen solution EPR spectra of Ru<sub>2</sub>(O<sub>2</sub>CC<sub>3</sub>H<sub>7</sub>)<sub>4</sub>Cl were used to derive g values and <sup>99</sup>Ru hyperfine coupling constants.<sup>23</sup> However, no accurate theoretical calculations have been reported to help interpret these data. The original proposal of a  $\sigma^2 \pi^4 \delta^2 \sigma_n^{1}$ - $\sigma_n'^1 \delta^{*1}$  ground state, <sup>14a</sup> with the high-spin character arising from close spacing of the  $\sigma_n$ ,  $\sigma_n'$ , and  $\delta^*$  orbitals, now seems untenable: all the recent theoretical and experimental work

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**Table II.** Total Energies,  $X\alpha$  Exchange Energies, and Virial Ratios<sup>*a*</sup>

	ΕŢ	$V_{\mathbf{X}\alpha}$	-2T/V
$Ru_2(O_2CH)_4$	-9638.9298	-350.3963	1.000 25
$Ru_2(O_2CH)_4^+$	-9638.8432	-350.1234	1.000 21
$Ru_2(O_2CH)_4Cl_2^-$	-10 558.1267	-406.1765	1.000 30
$Rh_2(O_2CH)_4$	-10 127.0066	-359.8986	1.000 30
$Rh_2(O_2CH)_4^+$	-10 126.8449	-359.5743	1.000 27
$Rh_2(O_2CH)_4(H_2O)_2$	-10 280.9064	-378.4538	1.000 11
$Rh_2(O_2CH)_4(H_2O)_2^+$	-10 280.7146	-378.3331	1.000 13

<sup>a</sup> Spin-polarized results in hartrees. Note that these quantities do depend on choice of bond lengths and sphere radii; see Computational Section for details of these choices.

on related systems indicates that the  $\sigma_n$  and  $\sigma_n'$  orbitals (essentially nonbonding  $p_z d_{z^2}$  hybrids directed outward from the ends of the metal-metal axis) are much too high in energy to be occupied.

In this paper we offer detailed explanations for the preferred oxidation level and magnetic properties of ruthenium carboxylate dimers, based on comparative SCF-X $\alpha$ -SW calculations of  $Ru_2(O_2CH)_4Cl_2^-$ ,  $Ru_2(O_2CH)_4^+$ ,  $Ru_2(O_2CH)_4$ ,  $Rh_2(O_2CH)_4(H_2O)_2^+$ , and  $Rh_2(O_2CH)_4^+$ . We have briefly noted our essential conclusion about the ground-state electronic configuration of  $Ru_2(O_2CR)_4^+$  in our previous paper on Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub>, Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>, and Rh<sub>2</sub>.<sup>5</sup> The comparison of  $Ru_2(O_2CH)_4Cl_2^-$  and  $Ru_2(O_2CH)_4^+$  also allows analysis of the interactions between the Ru-Ru and Ru-Cl bonds, thus providing a second theoretical picture of the metal-metal trans influence. The calculations on Rh<sub>2</sub>- $(O_2CH)_4(H_2O)_2^+$ , compared with those on  $Rh_2(O_2CH)_4$ - $(H_2O)_{2,a}$  allow analysis of the observed <sup>15a, c</sup> differences in bond lengths between  $[Rh_2(O_2CCH_3)_4(H_2O)_2]ClO_4 \cdot H_2O$  and  $Rh_2(O_2CCH_3)_4(H_2O)_2$ . We also comment in this context on the recent<sup>15b</sup> structures of  $Rh_2(O_2CCH_3)_4L_2$ , L = py, NHEt<sub>2</sub>, CO, PR<sub>3</sub>, giving an interpretation of the observed Rh-Rh and Rh-L variation differing from that in the structural paper.

Our calculations lead to an assignment of the electronic spectra of  $Ru_2(O_2CR)_4^+$  complexes which differs from those previously proposed,<sup>14a,24,26</sup> and to the first assignment of the twice-reported<sup>24,25</sup> spectrum of  $Rh_2(O_2CR)_4^+$  in solution. We anticipate eventual tests of both assignments by single-crystal polarized spectra;<sup>27</sup> if correct, they bring some new perspective to the continuing discussion<sup>20</sup> of  $\delta \rightarrow \delta^*$  transitions in  $D_{4h}$  dimers. We have also calculated ESR parameters for  $Ru_2(O_2CH)_4Cl_2^-$ , using the X $\alpha$ -SW properties package,<sup>28</sup> for comparison with experiment.

#### **Computational Section**

Coordinates for  $Ru_2(O_2CH)_4Cl_2^-$ ,  $Ru_2(O_2CH)_4^+$ , and  $Ru_2(O_2CH)_4$  in atomic units were derived from the average crystallographic bond parameters<sup>14</sup> of  $[Ru_2(O_2CC_3H_7)_4]Cl$ , namely, Ru-Ru = 2.28, Ru-Cl = 2.59, Ru-O = 2.00, C-O= 1.27, and C-H = 1.08 Å and Ru-Ru-O angle =  $89.3^{\circ}$ , using the relation 1 bohr = 0.529 17 Å and  $D_{4h}$  symmetry. For  $Rh_2(O_2CH)_4(H_2O)_2^+ Rh-Rh = 2.32, Rh-OH_2 = 2.31, and$ Rh-O = 2.01 Å were taken from the crystal structure<sup>15c</sup> of  $[Rh_2(O_2CCH_3)_4(H_2O)_2]ClO_4 \cdot H_2O$ . Other dimensions and the H<sub>2</sub>O orientation were as for  $Rh_2(O_2CH)_4(H_2O)_2$ .<sup>5</sup> Dimensions for  $Rh_2(O_2CH)_4^+$  were as for  $Rh_2(O_2CH)_4$ ;<sup>5</sup> we were unaware of the structure of  $[Rh_2(O_2CCH_3)_4(H_2O)_2]$ - $ClO_4 \cdot H_2O$  at this time. Overlapping atomic sphere radii were obtained nonempirically,<sup>29</sup> as 91% of the atomic-number radii, except for  $Rh_2(O_2CH)_4^+$ , where 89.3% was used. Touching outer-sphere radii were employed. Sphere radii and SCF charges in the various regions are summarized in Table I (available as supplementary material).

In other respects the calculations were carried out as for  $Mo_2(O_2CH)_4$ .<sup>3b</sup> For  $Ru_2(O_2CH)_4Cl_2^-$ , spherical harmonics through l = 1 were used on Cl, and a 1+ "Watson sphere"<sup>30</sup> was used to simulate the stabilizing effect of the surrounding crystal lattice. Both spin-restricted and spin-polarized ground-state SCF calculations were done for all species, since all were expected to be paramagnetic. Spin-polarized transition-state calculations of electronic transition energies were carried out for  $Ru_2(O_2CH)_4Cl_2^-$  and  $Rh_2(O_2CH)_4(H_2O)_2^+$ . The SCF potential for  $Ru_2(O_2CH)_4Cl_2^-$ , together with estimates of electronic transition energies, was used to calculate ESR parameters for  $Ru_2(O_2CH)_4Cl_2^-$ .

## Results

The energy level diagrams, as for other  $M_2(O_2CH)_4$  species,3b,5 contain three distinct regions. Twenty essentially unperturbed formate C-H and C-O  $\sigma$  orbitals lie in the ranges -1.25 to -0.65 hartree for Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub><sup>+</sup> and Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>- $(H_2O)_2^+$  and -1.10 to -0.50 hartree for Watson-sphere stabilized Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup>. Mainly C-O  $\pi$ , metal-O  $\sigma\pi$ , and O nonbonding orbitals follow next in energy, intermixed with primarily metal-metal orbitals; the highest occupied orbitals are always partially filled mainly metal-metal  $\pi^*$  and  $\delta^*$ . There is a large energy gap between these and the completely empty orbitals, which are, in order of increasing energy, mainly metal-metal  $\sigma^*$ , metal-O  $\sigma^*$  (two orbitals), and C-O  $\pi^*$  (four orbitals). For  $Ru_2(O_2CH)_4Cl_2^-$  and  $Rh_2(O_2CH)_4^ (H_2O)_2^+$ , additional orbitals correlating best with the  $\sigma$  and  $\pi$  lone pairs of Cl<sup>-</sup> and H<sub>2</sub>O, respectively, are found in the second region, those for Cl<sup>-</sup> lying about 0.12 hartree higher relative to the  $M_2(O_2CH)_4$  levels than those for  $H_2O_2$ .

Table II compares the total energies, exchange energies, and virial ratios for the calculated SCF ground states of all species. The first excited state for  $Ru_2(O_2CH)_4$ ,  $5e_g^22b_{1u}^2$ , is particularly close to the  $5e_g^{3}2b_{1u}^{1}$  ground state; the calculated separation in total energy is only ca. 2 kcal/mol. Energies and charge distributions for upper valence levels are given in Table III for  $Ru_2(O_2CH)_4^+$  and  $Ru_2(O_2CH)_4Cl_2^-$ , and in Table IV for  $Rh_2(O_2CH)_4(H_2O)_2^+$ . Figure 1 compares the energy levels of  $Ru_2(O_2CH)_4$ ,  $Ru_2(O_2CH)_4^+$ , and  $Ru_2(O_2CH)_4Cl_2^-$ , with emphasis on those important for Ru-Ru and Ru-Cl bonding. Figure 2 presents a similar comparison for  $Rh_2(O_2CH)_4$ - $(H_2O)_2$  and  $Rh_2(O_2CH)_4(H_2O)_2^+$ . Wave function contour maps comparing important metal-metal and metal-(axial ligand) orbitals of  $Ru_2(O_2CH)_4Cl_2^-$  and  $Rh_2(O_2CH)_4(H_2O)_2^+$ appear in Figures 3-5. Our assignment for the electronic spectra of Ru<sup>2.5+</sup> and Rh<sup>2.5+</sup> carboxylates appears in Tables V and VI, respectively.

#### Discussion

**Magnetic Properties of Ru** Carboxylates. As shown in Figure 1, the predicted Ru-Ru bond order in Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub><sup>+</sup> and Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup> is 2.5. The three unpaired electrons observed experimentally<sup>23</sup> are also predicted explicitly by the spin-polarized calculations. The high-spin,  $S = \frac{3}{2} e_g^2 b_{1u}^{-1} (\pi^{*2} \delta^{*1})$  configuration is favored over  $S = \frac{1}{2}$  alternatives by close spacing of the  $\pi^*$  and  $\delta^*$  orbitals. We now examine reasons for this close spacing, and for the related fact that the  $\delta^*$  level lies slightly higher in energy than the  $\pi^*$  level for these Ru and Rh carboxylates.

The ordering  $\delta^* < \pi^*$  is expected if metal-metal bonding entirely determines it. Consistently, we find this ordering in Rh<sub>2</sub> and Rh<sub>2</sub><sup>4+</sup>, where only metal-metal bonds are present,<sup>5</sup> and in Mo<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>, where the Mo-Mo bonding is so strong that it dominates other factors.<sup>3</sup> We see three factors interacting to produce the inversion in the Ru and Rh carboxylates: (1) downward shift of metal 4d levels relative to ligand levels from Mo to Ru to Rh; (2) influence of the carboxylate ligands; (3) influence of the axial ligands. Let us eliminate (3) for the

$\underline{\qquad \qquad } Ru_2(O_2CH)_4^+$						R	u <sub>2</sub> (O <sub>2</sub> CH) <sub>4</sub>	$Cl_2^-$				
$D_{4h}$		% c	harge <sup>b</sup>	major Ru		$D_{4h}$			% charge <sup>b</sup>		major Ru	
level	energy	2Ru	$4O_2CH$	basis fns <sup>c</sup>	main type	level	energy	2Ru	$4O_2CH$	2C1	basis fns <sup>c</sup>	main type
2820	+0.0025		100	)	1	2822	-0.0043		100		)	
3b <sub>20</sub>	-0.0201	4	96	}	C-O π*	4b2g	-0.0065	4	96		}	C-O π*
$7e_{11}$	-0.0176	0	100	J		9e <sub>11</sub>	-0.0206	Ó	97	2		
5b10	-0.0870	59	41	$d_{y^2-y^2}$		5b10	-0.0846	61	39	_	$d_{x^2-y^2}$	
4b20	-0.1029	66	34	dx2-12*	Ru-O $\sigma^*$	4b <sub>20</sub>	-0.0992	67	33		dy2-12*	Ru-O σ*
$4a_{2u}$	-0.1627	84	16	d- 2*	Ru-Ru $\sigma^*$	$6a_{2u}$	-0.1140	75	12	12	d - 2*	Ru-Ru σ*,
				-							-	Ru-Cl σ*
2b1u <sup>d</sup>	-0.2250	69	31	$d_{xv}$ *	Ru-Ruδ*	$2b_{1u}^{d}$	-0.2214	71	29		$d_{xy}$ *	Ru−Ruð*
5eg <sup>d</sup>	-0.2347	89	11	dx2.12*	Ru-Ru $\pi^*$	$6e_g^d$	-0.2224	85	6	9	$d_{xz,yz}$ *	Ru-Ru $\pi^*$
Ū.						$7a_{1g}$	-0.2421	23	5	72	$d_z 2$ , $p_z$	Ru-Cl $\sigma^*$ .
						c						Ru-Ruσ
2b <sub>2g</sub>	-0.2672	84	16	$d_{xv}$	Ru-Ruδ	$2b_{2g}$	-0.2621	85	15		$d_{xy}$	Ru-Ruð
				-		7en	-0.2653	16	8	76		
						5eg	-0.2755	6	8	86	ì	Cl $\pi$ lone
						-					ſ	pair
						5a <sub>2u</sub>	-0.2891	9	9	82	$d_{z^2}$ , * s*, $p_z$ *	Ru–Cl $\sigma$
6e <sub>u</sub>	-0.2860	30	70	$d_{xz,yz}$ , $p_{x,y}$	Ru–O $\pi$	6e <sub>u</sub>	-0.2924	24	56	20	$\mathbf{d}_{xz,yz}, \mathbf{p}_{x,y}$	Ru–O $\pi$
la <sub>lu</sub>	-0.3013		100			la <sub>iu</sub>	-0.3046		100		)	
4eg	-0.3104	8	92	}	• O lone pair	4eg	-0.3141	7	89	4	}	O lone pair
3eg	-0.3246	6	94	J		3eg	-0.3272	5	94	1	J	
5eu	-0.3389	71	29	$d_{xz,vz}$	Ru-Ru $\pi$	5e <sub>u</sub>	-0.3385	63	34	3	$d_{xz,yz}$	Ru-Ru $\pi$
5a <sub>1g</sub>	-0.3286	42	58	<b>s</b> , $d_{z^{2}}$	Ru–O $\sigma$ ,	6a <sub>1g</sub>	-0.3416	27	57	16	<b>s</b> , $d_{z^{2}}$	Ru-O $\sigma$ ,
					Ru-Ru $\sigma$							$Ru-Cl\sigma$
3a <sub>2u</sub>	-0.3549	18	82	dz 2*, s*		4a <sub>2u</sub>	-0.3595	19	75	6	$d_{z^{2}}$ , s*	Ru-O $\sigma$ ,
												Ru-Ru
					$R_{\rm H} = 0 \sigma \pi$			• •				$\sigma^*$
3b <sub>2u</sub>	-0.3662	21	79	$d_{x^2-y^2}$ *		36 <sub>2u</sub>	-0.3687	20	80		$d_{x^2-y^2}$	Ru-O
lb <sub>1u</sub>	-0.3821	37	63	$d_{xy}^*$		lb <sub>(u</sub>	-0.3808	34	66		$d_{xy}^{*}$	σ, π
4b <sub>1g</sub>	-0.3885	34	66	$d_{x^2-y^2}$		40 <sub>1g</sub>	-0.3927	33	67		$d_{x^2-y^2}$	
la <sub>2g</sub>	-0.3921		100		$C-O\pi$	la <sub>2g</sub>	-0.3957		100		4	$C-O\pi$
4a)g	-0.3976	13	27	$d_z^2$	$Ru-Ru\sigma$ ,	$5a_{1g}$	-0.4029	66	24	10	<b>d</b> <sub>z</sub> 2	$Ku-Ku\sigma$ ,
4	0.4104	2	0.0		Ku-Oσ	4.	0.4121		0.0	0		$Ru - O\sigma$
$4e_u$	-0.4104	2	98	,	$C-O\pi$	$4e_{u}$	-0.4131	17	99	0	L	$C = 0\pi$
Ib <sub>2g</sub>	-0.4513		81	<b>d</b> <sub>xy</sub>	$\kappa_{u-OC}\pi$	ID2g	-0.451/	17	83		a <sub>xy</sub>	$\kappa u - OC \pi$

Table III, Spin-Restricted Upper Valence Levels (hartrees)<sup>a</sup> and Charge Distributions for Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub><sup>+</sup> and Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup>

<sup>a</sup> All levels above -0.5 hartree except for diffuse Rydberg-state orbitals. These occur for  $Ru_2(O_2CH)_4Cl_2^-$  at -0.0758 ( $8a_{1g}$ ), -0.0644 ( $8e_u$ ), -0.0580 ( $7a_{2u}$ ), -0.0554 ( $3b_{2g}$ ), -0.0360 ( $7e_g$ ), -0.0217 ( $6b_{1g}$ ), -0.0183 ( $9a_{1g}$ ), and -0.0123 ( $3b_{1u}$ ). Only 3-10% of their charge is located within the atomic spheres; 0.15 hartree has been added to the actual  $Ru_2(O_2CH)_4^+$  eigenvalues to make the 20 formate-localized orbitals below -0.5 hartree essentially coincident in the two complexes. <sup>b</sup> *Relative* amounts of charge within the atomic spheres. The only  $Ru_2(O_2CH)_4Cl_2^-$  orbitals with less than 77% of the total charge within the atomic spheres are the unoccupied  $9e_u$ ,  $4b_{2g}$ , and  $2a_{2g}$  (35-57%). <sup>c</sup> Spherical harmonics contributing more than 10% of the Ru charge for important Ru-Ru, Ru-Cl, and Ru-O\_2CH orbitals, listed in order of decreasing importance. All such Ru contributions are more than 80% d except for the following:  $Ru_2(O_2CH)_4Cl_2^-$ ,  $6a_{1g}$  (67% s, 30%  $d_{22}$ ) and  $7a_{1g}$  (68%  $d_2$ , 24%  $p_z$ );  $Ru_2(O_2CH)_4^+$ ,  $5a_{1g}$  (52% s, 42%  $d_z^2$ ). Asterisks indicate antibonding combinations, no asterisks bonding combinations. <sup>d</sup> Half-occupied levels. Those below are completely filled, those above completely empty. In the spin-polarized calculation for  $Ru_2(O_2CH)_4Cl_2^-$ , the occupied  $2b_{1u}^+$  and  $6e_g^+$  are 66% Ru and 74% Ru/20% Cl, respectively, while the empty  $2b_{1u}^+$  and  $6e_g^+$  are 74% Ru and 89% Ru/6% Cl, respectively. Other orbitals with more than 10% difference between the spin-up and -down Ru contributions are  $5a_{1g}$  ( $^+72\%$ ,  $\downarrow 61\%$ ),  $1b_{1u}$  ( $^+41\%$ ,  $\downarrow 30\%$ ).  $5e_u$  ( $^+74\%$ ,  $\downarrow 53\%$ ), and  $7e_u$  ( $^+8\%$ ,  $\downarrow 23\%$ ).

moment, and emphasize (1) and (2), by comparing in sequence the calculated energy level diagrams for  $Mo_2(O_2CH)_4$ ,  $Ru_2(O_2CH)_4$ ,  $Ru_2(O_2CH)_4^+$ ,  $Rh_2(O_2CH)_4(H_2O)_2$ , and  $Rh_2(O_2CH)_4(H_2O)_2^+$  (ref 2 and Figures 1 and 2), using the  $6b_{2g}$  level for the last two to represent the  $\pi^*$  energy ( $6b_{3g}$  interacts with the axial  $H_2O \pi$  lone pairs).

The essential point is that the  $\delta^*$  d-orbital combination interacts significantly with lower lying carboxylate orbitals, while the  $\pi^*$  does not. The  $1b_{1u}$  orbital (in  $D_{4h}$ ;  $5b_{1u}$  for  $D_{2h}$ ) is one of the eight mainly ligand orbitals which best correlate with the eight metal-oxygen bonds;<sup>3b</sup> its metal character is 14, 27, 37, 37, and 45% along the above series (ref 2b and Tables III and IV). By contrast the  $3e_g$  and  $4e_g$  orbitals (in  $D_{4h}$ ;  $3,4b_{3g}$ and  $4,5b_{2g}$  in  $D_{2h}$ ) are best identified with oxygen lone pairs; their metal character varies from 1-2% in Mo<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub> to 11-16% in Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub><sup>+</sup>. Thus, as the metal 4d *atomic* orbitals drop in energy along the sequence Mo<sup>2+</sup>, Ru<sup>2+</sup>, Ru<sup>2.5+</sup>, Rh<sup>2+</sup>, Rh<sup>2.5+</sup>, the *molecular* orbital best classified as metal-metal  $\delta^*$  does not drop as fast as  $\pi^*$ , because unlike  $\pi^*$  it is the antibonding orbital of a significant metal-carboxylate interaction. A good single illustration of this point is the comparative  $\delta^*$  and  $\pi^*$  energies for Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub> and Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub><sup>+</sup> in Figure 1.

The influence of the axial ligands is the opposite of the carboxylates. The  $\pi^*$  rather than the  $\delta^*$  orbitals are destabilized more by interaction with ligand orbitals. The important lower lying ligand orbitals are the  $p\pi$  lone pairs of Cl<sup>-</sup> and H<sub>2</sub>O; some are of  $\pi^*$ , but none are of  $\delta^*$ , symmetry. Thus, as shown in Figures 1 and 2, and in Figure 1 of ref 5, the addition of axial ligands decreases the  $\delta^{*-}\pi^*$  splitting in the Ru and Rh dimers. In no case do the calculations predict a restoration of the ordering  $\delta^* < \pi^*$ , but the resulting splittings are quite small, and the theory could well be in error by such amounts.

Finally, there is a related effect of metal-metal distance on the  $\delta^{*-}\pi^{*}$  splitting. This is shown by the energy level diagrams for Cr<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub> at 2.20 and 2.36 Å;<sup>17</sup> the  $\delta^{*} < \pi^{*}$  ordering at the shorter distance is reversed at the longer. Presumably

**Table IV**, Spin-Restricted Upper Valence Levels (hartrees)<sup>*a*</sup> and Charge Distribution for  $Rh_2(O_2CH)_4(H_2O)_2^+$ 

Don			% charge	ь	major Rha	
level	energy	2Rh	40 <sub>2</sub> CH	$2H_2O$	basis fns	main type
	±0.0278	0	100		)	1
(0h.	$\pm 0.0278$	U	100			
190 <sub>2u</sub>	$\pm 0.0171$	1	08	1		C-O π*
(903u	-0.0000	1	06	0		
11ag 6h	-0.0030	55	45	U	a /	
50 50	-0.0930	47	20		$d_{xy}$	Rh-Oσ*
Jau oh	-0.1110	74	30	10	d <sub>xy</sub> · )	Dh Dh 📲
oulu	-0.1291	/4	15	10	$\mathbf{q}_{z}$	Ph OH.
						κπ−0112 σ*
7h. d	-0.2231	63	37	Λ	dъ*	Rh_Rhδ*
(6b)	-0.2251	65	7	29	d * )	
1 6b.	-0.2290	83	17	2)	$d_{yz}$	Rh-Rh $\pi^*$
(7b	-0.2350	16	17	67	$\mathbf{u}_{xz}$	
1 5b.	-0.2451	17	30	53		$H_2 O \pi$ ione
( 503g	0.2031	47	17	20	ن د	pair
9a <sub>g</sub>	-0.2640	4/	17	36	$a_z 2$ , s, $p_z$	Rn-OH <sub>2</sub>
						$\pi^{\tau}$ , DL DL
						Rn-Rn
80	-0.2646	<b>Q</b> 1	19	r	d	0 Ph Ph S
oag (7h	-0.2646	21	10	2	$d_{x^2-y^2}$	
103u	-0.2646	21	79	22	$\mathbf{u}_{xz}, \mathbf{p}_x$	
(00 <sub>2u</sub>	-0.2716	9	100	22	,	KII-O #
48 <sub>0</sub>	-0.2770	11	100	0		
1 3 0 2g	-0.2882	11	89 70	0		O lone pair
(403g	-0.2913	14	/9	0		
402g	-0.3033	11	00	2	,	
( 303g	-0.3041	10	83 70	21	* 1 *	Ph O a
001u	-0.3226	9	10	21	S*, U <sub>Z</sub> 2**	Dh* Dh
1003u	-0.3223	70	19	1	d <sub>xz</sub>	
(30 <sub>2u</sub>	-0.3270	/0	18	4	$u_{yz}$	Ж
7ag	-0.3320	15	64	21	$\mathbf{s}, \mathbf{d}_{z^2}$	
3a <sub>u</sub>	-0.3476	25	75		$d_{xy}$ *	Rh-Οσ.
61	0 2616	15		0	L.	$\pi$
501u	-0.3615	45	22	U	$d_{x^2-y^{2*}}$	
501g	-0.3648	39	61		$a_{xy}$	
401g	-0.3669	20	100	(5	<b>.</b>	$C = 0 \pi$
40 <sub>1u</sub>	-0.3694	22	13	65	$a_{z^2}, p_{z^*}$	Rn-OH <sub>2</sub>
						$\sigma_{\rm r}$
						KN-KN
(56	_0.2062					σ
1 303u	-0.2852	n	0.0	0		C 0 =
(40 <sub>2u</sub>	-0.4009	50	98	26	d .	
oag	-0.4098	39	3	30	$\mathbf{u}_{z^{2}}$	
						Kn-OH <sub>2</sub>
5.0	0 42(0	22	70	0	4	
Jag	-0.4260	22	/8	U	a <sub>xy</sub>	$\kappa_{n-OC}\pi$

<sup>a</sup> All levels above -0.48 hartree except for diffuse Rydberg-state orbitals, which occur at  $-0.0252 (10a_g)$ ,  $-0.0119 (8b_{3u})$ , -0.0118 $(8b_{2u})$ , -0.0056  $(9b_{1u})$ , +0.0221  $(7b_{2g})$ , and +0.0224  $(7b_{3g})$ . Only 5-11% of their charge is located within the atomic spheres. 0.15 hartree has been added to all actual eigenvalues to make the 20 formate localized orbitals below -0.48 hartree essentially coincident with those in  $Rh_2(O_2CH)_4(H_2O)_2$  and  $Ru_2(O_2CH)_4Cl_2^{-}$ . *b Relative* amounts of charge within the atomic spheres. The only orbitals with less than 83% of the charge there are unoccupied 7b1g, 9b2u, 9b3u, and 11ag (27-63%). <sup>c</sup> Spherical harmonics contributing more than 10% of the Rh charge for important Rh-Rh, Rh-OH<sub>2</sub>, and Rh-O<sub>2</sub>CH orbitals, listed in order of decreasing importance. All such Rh contributions are more than 78% d except for  $7a_g$  (59% s, 41% d<sub>z</sub><sup>2</sup>)  $6b_{1u}$  $(60\% \text{ s*}, 40\% \text{ d}_z 2^*)$ , and  $9a_g (69\% \text{ d}_z 2, 16\% \text{ s}, 15\% \text{ p}_z)$ . Asterisks indicate antibonding and no asterisks bonding combinations. <sup>d</sup> Halfoccupied level. Those below are completely filled, those above completely empty. In the spin-polarized calculation, the occupied  $7b_{1u}$ is 62% Rh and the empty  $7b_{1u}\downarrow$  64% Rh. The only orbital with more than 5% difference between the spin-up and -down Rh contributions is  $6b_{3g}$  († 61% Rh/33% H<sub>2</sub>O,  $\downarrow 68\%$  Rh/25% H<sub>2</sub>O).

the reason is increasing Cr-O bond strength. The stronger the Cr-O bonds, the greater the destabilization of  $\delta^*$  relative to  $\pi^*$ .



Figure 1. Spin-restricted SCF energy levels for Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>, Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub><sup>+</sup>, and Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup> above -0.51 hartree, and the highest occupied and lowest unoccupied spin-polarized levels for the last. The levels best described as Ru-Ru  $\sigma$ ,  $\pi$ ,  $\delta$ ,  $\delta^*$ ,  $\pi^*$ , and  $\sigma^*$ , Ru-Cl  $\sigma$  and  $\sigma^*$ , and Cl  $p\pi$  lone pairs are indicated. Mulliken symbols are given for these levels, and for all others of Ru-Ru  $\sigma$ ,  $\pi$ ,  $\pi^*$ , and  $\sigma^*$  symmetry (a<sub>1g</sub>, e., e.g., and a<sub>2u</sub>, respectively). The occupation of the highest filled or partially filled levels is shown.



Figure 2. Spin-restricted SCF energy levels for Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub> and Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub><sup>+</sup> above -0.48 hartree, and the highest occupied and lowest unoccupied spin-polarized levels for the latter. The levels best described as Rh-Rh  $\sigma$ ,  $\pi$ ,  $\delta$ ,  $\delta^*$ ,  $\pi^*$ , and  $\sigma^*$ . Rh-OH<sub>2</sub>  $\sigma$  and  $\sigma^*$ , and H<sub>2</sub>O  $p\pi$  lone pairs are indicated. Mulliken symbols are given for these levels, and for all others of Rh-Rh  $\sigma$  and  $\sigma^*$  symmetry (ag and b<sub>1u</sub>, respectively). The occupation of the highest filled or partially filled levels is shown.

The conclusion of general value from this analysis, which could not have been reached without the calculations, is that for these weaker metal-metal bonds the relative ordering of



Figure 3. Contour maps of the wave functions for the important metal-metal  $\sigma$  orbitals of Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup> and Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub><sup>+</sup>, showing the bonding of the trans ligands in a<sub>1g</sub>/a<sub>g</sub> symmetry. These maps and those of Figure 4 and the left half of Figure 5 are in the plane of two of the formate groups. For Figures 3-5 the contour values are 0, ±1, ±2, ±3, ±4, ±5 = 0, ±0.02, ±0.09, ±0.13, ±0.17, respectively, and inner contours close to the atomic centers are omitted for clarity.

 $\pi^*$  and  $\delta^*$ , and their exact separation, is greatly influenced by the ligands present. In other words, Ru<sup>2.5</sup>-Ru<sup>2.5</sup>  $D_{4h}$  dimers with other ligands might well have a different net spin and orbital occupation. Recently, the first such compounds, Ru<sub>2</sub>(N<sub>4</sub>C<sub>22</sub>H<sub>22</sub>)<sub>2</sub><sup>0,+,2+</sup>, have been characterized.<sup>31</sup> The ligand is a tetradentate macrocycle and the crystal structure of the Ru<sup>2.5+</sup> ion shows a nonbridged, approximately  $D_{4h}$  dimer with Ru-Ru = 2.26 Å (cf. 2.25-2.29 Å in the carboxylates). The 0, 1+, and 2+ species contain two, one, and zero unpaired electrons, respectively. As the authors of ref 31 point out, the reasonable electronic configurations implied by this data are  $\delta^{*2}\pi^{*2}$ ,  $\delta^{*2}\pi^{*1}$ , and  $\delta^{*1}\pi^{*0}$ , respectively. The conclusion is that the  $\delta^*$  level lies considerably below  $\pi^*$  in this case.

Stable Oxidation Level of Ru and Rh Carboxylates. Any half-filled set of degenerate orbitals has special stability relative

to surrounding configurations, since this is a favorable situation for exchange energy. The calculations thus suggest that one major contribution to the stability of  $Ru_2(O_2CR)_4^+$  relative to  $Ru_2(O_2CR)_4$  is the half-filled  $\pi^*$  set attained in the former (see Figure 1). There is no such stabilizing factor for  $Rh_2(O_2CR)_4^+$  relative to  $Rh_2(O_2CR)_4$ , since the two extra electrons added from Ru to Rh fill the  $\pi^*$  orbital completely (see Figure 2). We have explicitly verified this suggestion by comparing exchange energies and total energies of  $M_2(O_2CH)_4^{0,+}$ , M = Ru, Rh (see Table II). The positive ion is indeed predicted to be much more stable relative to the neutral species in the Ru case, and about  $\frac{2}{3}$  of the extra stability can be traced to the exchange energy.

The other point to be made in this connection is that the neutral Ru species is predicted to be susceptible to Jahn-Teller



Figure 4. Contour maps of the wave functions for the important metal-metal  $\sigma^*$  orbitals of  $Ru_2(O_2CH)_4Cl_2^-$  and  $Rh_2(O_2CH)_4(H_2O)_2^+$ , showing the bonding of the trans ligands in  $a_{2u}/b_{1u}$  symmetry.

distortion (see Figure 1). This would take the form of elongation of Ru-O distances in one plane and shortening in the other. The neutral species would thereby become more thermodynamically stable, but perhaps also more reactive toward decomposition of the cage structure. The neutral species prepared by electrochemical reduction of the cation in solution is indeed observed to decompose at an appreciable rate.<sup>23</sup>

These ideas suggest an explanation for the unusual conditions required for success in the original synthesis of  $Ru_2(O_2CR)_4Cl$ . Although the overall reaction was a reduction from  $Ru^{3+}$  in  $RuCl_3$  to  $Ru^{2.5+}$  in the dimer, an *oxygen* atmosphere was necessary to obtain a good yield.<sup>21a</sup> Possibly the role of  $O_2$  is to keep ruthenium from being reduced below oxidation state 2.5, so as to avoid the irreversible decomposition of the cage structure. A newer synthesis<sup>21b</sup> uses excess  $Cl^-$  in place of  $O_2$ , which again should stabilize  $Ru_2(O_2CR)_4^+$  relative to  $Ru_2(O_2CR)_4$ . (Cl-Ru-Ru-Cl)<sup>3+</sup> vs. (H<sub>2</sub>O-Rh-Rh-OH<sub>2</sub>)<sup>5+</sup>. The four orbitals of Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup> which correlate best with the Cl<sup>-</sup> lone pairs are, in order of increasing energy,  $5a_{2u}$ ,  $5e_g$ ,  $7e_u$ , and  $7a_{1g}$  (see Figure 1). The first two have Ru-Cl bonding character, and the last two Ru-Cl antibonding character, because the lone-pair combinations of  $a_{2u}$  and  $e_g$  symmetry are lower in energy, while those of  $e_u$  and  $a_{1g}$  symmetry are higher in energy, than the Ru-Ru orbitals with which they interact ( $\sigma^*$ ,  $\pi^*$ ,  $\pi$ , and  $\sigma$ , respectively). The ordering reflects this difference in character, and also the fact that the Ru-Cl  $\sigma$  interaction (involving Ru-Ru  $\sigma$  and  $\sigma^*$  orbitals) is stronger than the Ru-Cl  $\pi$  interaction (involving Ru-Ru  $\pi$  and  $\pi^*$  orbitals).

We first consider whether the  $\pi$  interaction is important. Since the Ru-Ru  $\pi^*$  orbitals are only half filled, there is an opportunity for net Cl  $\pi \rightarrow$  Ru-Ru  $\pi^*$  charge transfer, which would strengthen the Ru-Cl bonds at the expense of the Ru-Ru bond. However, the orbital overlap is small, as shown



Figure 5. Contour maps of the wave functions of the important metal-metal  $\pi^*$  orbitals of Ru<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>Cl<sub>2</sub><sup>-</sup> and Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub><sup>+</sup> which can interact with the  $p\pi$  lone pairs of the trans ligands. The plane for the Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub><sup>+</sup> maps lies halfway between those of the formate groups, and perpendicular to that of the water molecules.

in Figure 5. The Ru-Cl  $\pi$  overlap in 5eg may be compared with the main Ru-Cl  $\sigma$  overlaps, which occur in 4,5a<sub>2u</sub> (Figure 4) and arise from Cl  $\sigma \rightarrow$  Ru-Ru  $\sigma^*$  donation. There appears to be about an order of magnitude less  $\pi$  than  $\sigma$  overlap *charge* (wave function squared). Since the Ru-Cl  $\sigma$  bonding is already weak compared to normal bonds, we neglect the net Ru-Cl  $\pi$ bonding as unimportant in our subsequent discussion of the Cl<sup>-</sup> trans influence.

This is not to say that there is not considerable polarization of the Cl<sup>-</sup>  $\pi$  lone pairs by the Ru-Ru  $\pi$  and  $\pi^*$  electrons, and vice versa. For example, the mainly-Cl 7e<sub>u</sub> orbital has 16% Ru character. In Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub><sup>+</sup>, despite the completely filled  $\pi^*$  orbitals and resultant impossibility of *net* H<sub>2</sub>O  $\pi \rightarrow$ Rh-Rh  $\pi^*$  charge transfer, there is even more pronounced orbital mixing; e.g., the mainly Rh-Rh  $\pi^*$  6b<sub>3g</sub> orbital has 29% H<sub>2</sub>O character. Such polarization is important in its influence on the *character* of highest occupied orbitals and molecular properties which reflect this. However, it should not be confused with bonding—i.e., with strong orbital overlap and, especially when both bonding and antibonding orbitals are filled, with net charge transfer.

The  $(Cl-Ru-Ru-Cl)^{3+}$  and  $(H_2O-Rh-Rh-OH_2)^{5+} \sigma$ systems have much in common. As for  $Rh_2(O_2CH)_4(H_2O)_2$ ,<sup>5</sup> in both  $a_{1g}/a_g$  (M-M  $\sigma$ ) and  $a_{2u}/b_{1u}$  (M-M  $\sigma^*$ ) symmetries, the  $M_2(O_2CH)_4$  unit contributes two orbitals and the axial ligand L one to the bonding. The three MOs which result in the present cases are depicted in Figure 3 for  $a_{1g}/a_g$  and Figure 4 for  $a_{2u}/b_{1u}$ . Our previous general conclusions about the mutual influence of the M-M and M-L bonds<sup>5</sup> apply equally well to the present cases, and will not be repeated here.

The question we wish to discuss is which ligand, Cl<sup>-</sup> or H<sub>2</sub>O, is more effective at weakening the M-M  $\sigma$  bond by trans

coordination. As is evident from Figures 3 and 4, the presence of the carboxylates complicates the picture. For this reason we present in 2 interaction diagrams based on the calculations,



but simplified to omit the carboxylate orbitals. The clear difference between  $Cl^-$  and  $H_2O$  is the higher relative energy of the  $Cl^- \sigma$  lone pairs. This has several consequences for the M-M bond strength, which we now explore.

The important first-order M-M bond weakening upon trans ligand coordination results from ligand lone pair donation into the M-M  $\sigma^*$  orbital. The magnitude of the donation is reflected in the MOs by the amount of M-M  $\sigma^*$  character found in *filled* orbitals of  $a_{2u}/b_{1u}$  symmetry. From the diagram above, one expects Cl<sup>-</sup> to be a more effective donor than H<sub>2</sub>O, all other things being constant, since its lone pairs are closer in energy to the M-M  $\sigma^*$  orbital. However, Figure 4 indicates that the two are about equally effective in the two cases at hand. H<sub>2</sub>O introduces more  $\sigma^*$  character into the lower of the two filled orbitals (4a<sub>2u</sub>, 4b<sub>1u</sub>), but Cl<sup>-</sup> more into the upper one (5a<sub>2u</sub>, 6b<sub>1u</sub>). The point is that all other things are *not* constant: the Ru<sup>2.5+</sup>-Ru<sup>2.5+</sup> bond is stronger, and should be harder to

Table V.	Electronic S	pectra of Ru <sup>2.5+</sup>	Carboxylates	$(\mu m^{-1})$
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D <sub>4h</sub> transition	selection rule	type <sup>a</sup>	Calcd, bRu2(O2CH)4Cl2-	exptl, <sup>c</sup> [Ru <sub>2</sub> (O <sub>2</sub> CCH <sub>3</sub> ) <sub>4</sub> ]Cl	$exptl,^d$ Ru <sub>2</sub> (O <sub>2</sub> CCH <sub>3</sub> ) <sub>4</sub> (H <sub>2</sub> O) <sub>2</sub> <sup>+</sup>
$2b_{2g} \rightarrow 6e_g$	forbidden	$\delta \rightarrow \pi^*$	0.86		0.90 ((60)
$2b_{2g} \rightarrow 2b_{1u}$	allowed z	δ → δ*	0.88		1.04∫ <sup>(€ 00)</sup>
7eu → 6eg	allowed z	$Cl \rightarrow \pi^*$	1.35		
$5e_g \rightarrow 2b_{1u}$	allowed xy	$Cl \rightarrow \delta^*$	1.60		
$5a_{2u} \rightarrow 6e_g$	allowed $xy$	$Cl \rightarrow \pi^*$	1.87	1.76 sh	
6e <sub>u</sub> → 6e <sub>g</sub>	allowed z	$O\pi \rightarrow \pi^*$	1.99	2.16	2.35 (e 700)
la <sub>1u</sub> → 6e <sub>g</sub>	allowed xy	$O \rightarrow \pi^*$	2.30		
$6e_g \rightarrow 6a_{2u}$	allowed <i>xy</i>	$\pi^* \rightarrow \sigma^*$	2.41		
$4e_g \rightarrow 2b_{1u}$	allowed <i>xy</i>	O → δ*	2.47		

<sup>*a*</sup>  $\delta$ ,  $\delta^*$ ,  $\pi^*$ , and  $\sigma^*$  denote the Ru- Ru character of mainly Ru orbitals. Cl and O denote predominantly Cl and O lone pair orbitals, respectively. O $\pi$  is a predominantly oxygen orbital with significant (24%) Ru-Ru  $\pi$  character (see Table III). <sup>*b*</sup> All spin- and dipole-allowed transitions between 0.8 and 2.7  $\mu$ m<sup>-1</sup>, and the lowest lying spin-allowed, dipole-forbidden transition in this range, from spin-polarized calculations. <sup>*c*</sup> Band maxima in diffuse reflectance spectrum of solid (ref 26), from 1.4 to 3.2  $\mu$ m<sup>-1</sup>. Continuously rising intensity is observed above 2.5  $\mu$ m<sup>-1</sup> which does not peak below the experimental limit. <sup>*d*</sup> Band maxima and molar absorptivities of [Ru<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>]Cl in aqueous solution (ref 24), from 0.8 to 3.3  $\mu$ m<sup>-1</sup>. Continuously rising intensity is observed above 2.7  $\mu$ m<sup>-1</sup> which does not peak below the experimental limit.

**Table VI**, Electronic Spectra of  $Rh_2(O_2CR)_4(H_2O)_2^{0,+}$  ( $\mu m^{-1}$ )

D <sub>2h</sub> transition	type <sup>a</sup>	$\frac{\text{Calcd},^{b}}{\text{Rh}_{2}(\text{O}_{2}\text{CH})_{4}(\text{H}_{2}\text{O})_{2}}$	$exptl,^{c}$ Rh <sub>2</sub> (O <sub>2</sub> CCH <sub>3</sub> ) <sub>4</sub> (H <sub>2</sub> O) <sub>2</sub>	$\begin{array}{c} \text{calcd}, {}^{b}\\ \text{Rh}_2(\text{O}_2\text{CH})_4(\text{H}_2\text{O})_2{}^+\end{array}$	exptl,dRh2(O2CCH3)4(H2O)2+
$8a_g \rightarrow 7b_{1u}$ $5b_{2g}, 4b_{3g} \rightarrow 7b_{1u}$ $4b_{2g}, 3b_{3g} \rightarrow 7b_{1u}$	$\begin{array}{l} \delta \to \delta^* \\ O \to \delta^* \\ O \to \delta^* \end{array}$			0.92 1.63 1.93	1.32 (¢ 308)
$6b_{3g}, 6b_{2g} \rightarrow 8b_{1u}$ $6b_{3g}, 6b_{2g} \rightarrow 5a_{1u}$	$\begin{array}{c} \pi^* \rightarrow \sigma^* \\ \pi^* \rightarrow \operatorname{Rh-O} \\ \sigma^* \end{array}$	1.97 2.47	1.71 (ε 241) 2.27 (ε 106)	2.28 2.68	1.94 ( $\epsilon$ 298) ~2.5 <sup>e</sup>

<sup>*a*</sup>  $\delta$ ,  $\delta^*$ ,  $\pi^*$ , and  $\sigma^*$  denote the Rh-Rh character of mainly Rh orbitals. O denotes a mainly formate-oxygen lone pair orbital. Rh-O  $\sigma^*$  is a mainly Rh orbital of  $\delta^*$  symmetry with respect to the Rh-Rh bond. <sup>*b*</sup> All spin- and  $D_{4h}$  symmetry dipole-allowed transitions between 0.5 and 2.8  $\mu$ m<sup>-1</sup> except  $5b_{3g} \rightarrow 7b_{1u}$  (H<sub>2</sub>O $\pi \rightarrow \delta^*$ ) for the cation, calculated ca. 1.1  $\mu$ m<sup>-1</sup>, which should be extremely weak due to poor orbital overlap. From spin-polarized transition-state calculations. Average energies are quoted where the lower orbital is either  $b_{2g}$  or  $b_{3g}$ . <sup>*c*</sup> Band maxima and molar absorptivities in aqueous solution, from ref 24. <sup>*d*</sup> Band maxima and molar absorptivities in 1 M CF<sub>3</sub>SO<sub>3</sub>H, from ref 24. <sup>*e*</sup> See Figure 2 in ref 25.

weaken, than the  $Rh^{2.5+}-Rh^{2.5+}$  bond. Thus, both the approximate interaction diagram and the quantitative calculations suggest that  $Cl^-$  is *intrinsically* a better M-M weakening trans ligand than H<sub>2</sub>O. At the time of this writing, the first experimental data which directly tests this hypothesis has just been obtained, namely, the comparative structures of  $Ru_2(O_2CR)_4(H_2O)_2^+$  and  $Ru_2(O_2CR)_4Cl_{1,2}^{0,-}$  (see 1 above).<sup>14b</sup> The Ru-Ru bond in the aquo complex is indeed shorter than the average for the chloro complexes, by 0.035 Å.

2 suggests two second-order differences between  $Cl^-$  and  $H_2O$  as trans ligands which are confirmed by the quantitative calculations. First,  $H_2O$  introduces M-M  $\sigma^*$  character into the filled orbitals at lower energies on the average than  $Cl^-$ , as confirmed by Figure 4. Second, M-M  $\sigma$  character shifts to lower average energies in the presence of trans  $Cl^-$  than trans  $H_2O$ , as confirmed by Figure 3. Both effects favor  $H_2O$  over  $Cl^-$  as a trans bond weakener, but they should be much less important than the first-order donation into the M-M  $\sigma^*$  orbital.

Finally, we note that the higher relative  $Cl^-$  lone pair energies result in the middle of the three orbitals in both symmetries being most important for Ru-Cl bonding, while the lowest is most important for Rh-OH<sub>2</sub> bonding (see Figures 3 and 4). This is reflected in the labels on the energy levels in Figures 1 and 2.

 $Rh_2(O_2CR)_4(H_2O)_2^+$  vs.  $Rh_2(O_2CR)_4(H_2O)_2$ . It is interesting to consider the effect of increased metal oxidation state on the axial L-M-M-L bonding. We believe that the observed structural differences between  $Rh_2(O_2CCH_3)_4(H_2O)_2$  and  $[Rh_2(O_2CCH_3)_4(H_2O)_2]C1O_4 \cdot H_2O^{15ac}$  are consistent with our calculated electronic structures. The observations are that the Rh-Rh, Rh-OH<sub>2</sub>, and Rh-O(acetate) distances are respectively 0.069 (2), 0.089 (10), and 0.025 (9) Å shorter in the cationic than in the neutral complex. The simple effects of *normal* bond strengthening and Rh covalent radius contraction due to the increased Rh positive charge may be approximately accounted for by subtracting the Rh-O(acetate) shortening *twice* from the Rh-Rh and *once* from the Rh-OH<sub>2</sub> shortening. This leaves  $\Delta$ Rh-Rh = -0.02 Å and  $\Delta$ Rh-OH<sub>2</sub> = 0.06 Å from neutral complex to ion.

We see the extra 0.06 Å Rh-OH<sub>2</sub> shortening as due to the fact that the Rh-OH<sub>2</sub> bond starts out so much weaker than the Rh-O(acetate) bond (in Rh<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub>, the Rh-OH<sub>2</sub> distance is 0.27 Å longer than the average Rh-O(acetate) distance.<sup>15a</sup> Bond distances are well-known to become rapidly more sensitive to bond strength as the bond strength decreases.<sup>32</sup> The fact that the Rh-Rh distance still *decreases* slightly in the face of the Rh-OH<sub>2</sub> shortening testifies to the weakness of the Rh-OH<sub>2</sub> interaction. The amount of Rh-Rh bond strength lost to the Rh-OH<sub>2</sub> bond upon oxidation is apparently less than the small amount gained by removal of the  $\delta^*$  antibonding electron.

These ideas are explicitly confirmed by comparison of wave function contour maps for  $Rh_2(O_2CH)_4(H_2O)_2$  and  $Rh_2(O_2CH)_4(H_2O)_2^+$ . Of particular importance are the maps of the  $4b_{1u}$  orbital (Figure 4 here and in ref 5), the key orbital for both Rh-OH<sub>2</sub> bonding and resulting Rh-Rh bond weakening. The increased Rh-OH<sub>2</sub> bonding overlap from neutral complex to ion is easily seen, but there is no comparable increase in Rh-Rh antibonding character.

 $Rh_2(O_2CCH_3)_4L_2$ , L = H<sub>2</sub>O, py, NHEt<sub>2</sub>, CO, PF<sub>3</sub>, P(OPh)<sub>3</sub>,

PPh<sub>3</sub>, P(OMe)<sub>3</sub>. In a recent paper,<sup>15b</sup> Christoph and Koh (hereafter CK) report the molecular structures of these complexes and use the variation in Rh-Rh distance along the series (from 2.39 to 2.46 Å) to develop ideas about the electronic structures which differ somewhat from our own. They see the ordering of Rh-Rh distances as requiring significant backdonation to CO and PR<sub>3</sub> from a high-lying orbital of  $e_u$  (i.e., Rh-Rh  $\pi$ ) rather than eg (i.e., Rh-Rh  $\pi^*$ ) symmetry. They believe that placement of the  $\pi^*$  orbitals above the  $\pi$  in energy-the intuitively expected ordering, and that found by our calculations—would require that  $Rh \rightarrow L \pi$  bonding be negligible and that the Rh-L  $\sigma$  overlaps for H<sub>2</sub>O, py, and NHEt<sub>2</sub> decrease significantly faster with distance than for CO and PR<sub>3</sub>. They recognize the weight of evidence for a single Rh-Rh bond in the carboxylate dimers from electronic spectra, ESR spectra, analogies with other compounds, and calculations.<sup>5,33</sup> This leads them to propose an energy level diagram with both  $\pi^*$  and  $\pi$  orbitals filled, but with  $\pi$  higher than  $\pi^*$  in energy

We believe that the structural data of CK are consistent, rather than inconsistent, with our calculated electronic structures, in particular with the ordering  $\pi < \pi^*$ . Our basic hypothesis is that the order of increasing Rh-Rh distance is the order of increasing Rh-L  $\sigma$  covalent bond strength. We agree with CK that nonnegligible Rh $\rightarrow$ L  $\pi$  donation is present for L = CO and PR<sub>3</sub>, but we believe that (1) this donation comes from the  $\pi^*$  rather than the  $\pi$  orbitals; (2) at the extremely long Rh-L distances in these compounds (averaging 0.22 Å longer than normal), the L $\sigma$  $\rightarrow$ Rh-Rh  $\sigma^*$  donation is stronger than the  $\pi$  back-donation for all ligands, and stronger for L = CO and PR<sub>3</sub> than for L = H<sub>2</sub>O, py, and NHEt<sub>2</sub>. We now present arguments supporting our view.

The very existence of the Rh-Rh bond requires that the Rh-Rh  $\pi^*$  orbitals have more  $\pi$  donor ability, and the Rh-Rh  $\pi$  orbitals less, than normal. The  $\pi$  bonding orbital will have charge concentrated between the metals, and thus away from the axial ligands, while its antibonding counterpart will have charge projected toward the ligands. Drago et al.<sup>34</sup> have demonstrated the back-bonding capability of  $Rh_2(O_2CC_3H_7)_4$ by measuring  $\Delta H_f$  of Rh<sub>2</sub>(O<sub>2</sub>CC<sub>3</sub>H<sub>7</sub>)<sub>4</sub>L<sub>2</sub> in solution. They are able to separate out a " $\sigma$  only" component of  $\Delta H_{\rm f}$  using E and C parameters, and thus determine when a significant  $\pi$  component is present. Even for L = py, not normally a  $\pi$  acceptor, some extra stabilization over the " $\sigma$  only"  $\Delta H_{\rm f}$  is found. As they point out, the reasonable explanation for this enhanced donating ability of the rhodium carboxylate dimers is the hybridization of the Rh-Rh  $\pi^*$  orbital toward the ligands due to the Rh-Rh bonding.

As CK emphasize, the magnitude of a donor-acceptor interaction is proportional to  $S^2/\Delta E$ , where S is the overlap and  $\Delta E$  is the energy separation of the interacting orbitals. The overlap factor clearly favors Rh-Rh  $\pi^*$  over Rh-Rh  $\pi$  for donation to L $\pi$  acceptor orbitals. Likewise, Rh-Rh bonding by itself will give  $\pi^*$  the more favorable  $\Delta E$  by establishing the energy order  $\pi < \pi^*$ . The specific requirement for  $\pi$  to become the donor orbital of choice is thus that it interact so much more strongly with *carboxylate* orbitals than does  $\pi^*$ that the overlap factor and  $\Delta E$  established by Rh-Rh bonding are completely overwhelmed. We find nothing in either our qualitative analysis or quantitative calculations of Rh<sub>2</sub><sup>4+</sup>, HCO<sub>2</sub><sup>-</sup>, or the complexes to suggest that such a dramatic effect should or does exist.

Our conclusion that the Rh $\rightarrow$ L  $\pi$  donation in these complexes involves the  $\pi^*$  orbital leads to the further deduction that the ordering of Rh-Rh distances is determined by the Rh $\leftarrow$ L  $\sigma$  rather than Rh $\rightarrow$ L  $\pi$  interactions. If the  $\pi$  interaction were dominant, surely Rh<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>(CO)<sub>2</sub> would have a shorter, rather than 0.034 Å longer, Rh-Rh distance than Rh<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub>. Moreover, as emphasized by CK themselves in their Figures 6 and 7,  $Rh \rightarrow L \pi$  bonding should decrease faster with distance than  $Rh \leftarrow L \sigma$  bonding, and we are dealing with Rh-L distances averaging 0.22 Å longer than normal. Finally, for the two ligands studied by both Drago et al.<sup>34</sup> and CK,<sup>15b</sup> py and P(OR)<sub>3</sub>, the former authors find the " $\sigma$  only"  $\Delta H_f$  to be about 70% of the total.

We believe that it is quite reasonable for the  $\sigma$  covalent components of these long Rh-L bonds to be stronger for CO and PR<sub>3</sub> than for H<sub>2</sub>O, py, and Et<sub>2</sub>NH. Considering the  $\sigma$ bond strength in terms of  $S^2/\Delta E$ , the ionization energies of the L $\sigma$  lone pairs (and hence, presumably,  $\Delta E$  with the Rh-Rh  $\sigma^*$  orbital) decrease in the order H<sub>2</sub>O > CO > PF<sub>3</sub> > py > P(OMe)<sub>3</sub> > Et<sub>2</sub>NH > PPh<sub>3</sub>. Hence the ordering the Rh-Rh distances is essentially the inverse of the  $\Delta E$  ordering, except that the trans influences of py and Et<sub>2</sub>NH are smaller than expected. We believe that this reflects the importance of the overlap factor; that, at the long Rh-L distances present, the more diffuse lone pairs of CO and PR<sub>3</sub> overlap more effectively with the Rh-Rh  $\sigma^*$  function than do the rather compact lone pairs of H<sub>2</sub>O, py, and Et<sub>2</sub>NH.

CK cite literature Rh-L  $S^2$  values<sup>35</sup> to support their view that the values of  $S^2/\Delta E$  for the Rh-L  $\sigma$  interaction do not increase in the order of the observed Rh-Rh distances. There are several problems with these  $S^2$  values. They were calculated at normal Rh-L distances, 0.22 Å shorter on the average than these in the complexes in question. They were calculated assuming Rh<sup>+</sup>, probably too high a charge; our calculations on Rh<sub>2</sub> (O<sub>2</sub>CH)<sub>4</sub> indicate about Rh<sup>0.25+</sup>. Most seriously, they were calculated assuming a pure Rh 5p atomic function as the acceptor orbital. The 5p orbitals are much more diffuse than the 4d orbitals which almost certainly compose most of the Rh-Rh  $\sigma^*$  orbital; our calculations indicate that this orbital is about 92%  $d_{z^2}$ , 5% s, and 3%  $p_z$ . The 5p-based  $S^2$  values will consequently be much less sensitive to L and the Rh-L distance than in the real situation. In other words, we do not see the literature  $S^2$  values as very relevant to the question of how strongly axial ligands interact with the orbitally complex Rh-Rh bond, with its myriad of possibilities for hybridization, and rehybridization upon interaction. We plan to explicitly calculate  $Rh_2(O_2CH)_4L_2$ , L = CO, PH<sub>3</sub>, in hopes of characterizing the L-Rh-Rh-L bonding in detail.

Electronic Spectra of  $Ru_2(O_2CR)_4^+$  Complexes. The visible diffuse reflectance spectrum<sup>26</sup> of solid Ru<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>Cl shows a single prominent band with a primary maximum at 2.16  $\mu$ m<sup>-1</sup> and a secondary maximum at 1.79  $\mu$ m<sup>-1</sup>. In aqueous solution, Ru<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>Cl is a 1:1 electrolyte,<sup>21a</sup> and the reported spectrum there<sup>21a,24</sup> is therefore almost certainly that of  $Ru_2(O_2CCH_3)_4(H_2O)_2^+$ . Like the solid-state spectrum, it contains a single prominent band, now with a single maximum at 2.36  $\mu$ m<sup>-1</sup>. As indicated in Table V, we assign this band in both the solid state and solution to an allowed  $O\pi \rightarrow \pi^*$ transition, where the " $O\pi$ " orbital is a mainly Ru-O bonding orbital with a significant Ru-Ru  $\pi$  bonding contribution. A possible explanation for the splitting into two components in the solid is lifting of the  $\pi$  and  $\pi^*$  orbital degeneracies by the low site symmetry of the crystal. Our calculated energy (1.99)  $\mu$ m<sup>-1</sup>) is essentially the average energy of the two experimental maxima (1.96  $\mu$ m<sup>-1</sup>). Another possibility is that the 1.79- $\mu m^{-1}$  maximum is due to a Cl $\rightarrow \pi^*$  or Cl $\rightarrow \delta^*$  transition (see Table V).

The prominent visible band was originally assigned as  $\delta \rightarrow \sigma_n$ , <sup>14a,24</sup> but, as indicated earlier, the  $\sigma_n$  orbitals are now generally believed not to exist in the proper energy range. Moreover, resonance Raman experiments have shown that the band corresponds to a dipole allowed transition,<sup>26</sup> which  $\delta \rightarrow \sigma_n$  ( $b_{2g} \rightarrow a_{1g}, a_{2u}$ ) is not. The investigators of the Raman spectrum proposed a  $\delta \rightarrow \delta^*$  assignment. Our calculations indicate that the  $\delta \rightarrow \delta^*$  transition lies at much lower energy. The  $\delta^2 \delta^{*1}$  configuration is one for which previous experience indicates

that the  $\delta \rightarrow \delta^*$  transition should be calculated accurately, in contrast to the low theoretical values for  $\delta^2 \delta^{*0}$  configurations.<sup>20,36,37</sup> Our predicted  $\delta \rightarrow \delta^*$  energy lies outside the experimental range for the solid-state spectrum of Ru<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>Cl, but it is close to the energy of a weak band in the solution spectrum, which we thus assign to  $\delta \rightarrow \delta^*$  (see Table V). The authors report that this band is actually composite, with two maxima. A forbidden transition,  $\delta \rightarrow \pi^*$ , is predicted close to  $\delta \rightarrow \delta^*$ , and we suggest that it may contribute to the observed intensity. Even in quadruply bonded dimers  $\delta \rightarrow \delta^*$  transitions are fairly weak, and it is perhaps not surprising that, at the longer metal-metal distance in the Ru(2.5) complexes, their intensity should be comparable to that of forbidden transitions.

Above 2.3  $\mu$ m<sup>-1</sup> the calculations predict a very large number of allowed transitions. The first few are listed in Table V. This is consistent with the experimental solution spectrum,<sup>21a</sup> which shows intense absorption (reaching  $\epsilon > 2000$ ) in the range 2.5-5.0  $\mu$ m<sup>-1</sup> that appears to be due to a number of overlapping transitions. We make no attempt to assign this complicated region of the spectrum.

Electronic Spectra of Rh<sub>2</sub>(O<sub>2</sub>CR)<sub>4</sub><sup>0,+</sup> Complexes. In our previous paper on Rh(II) carboxylate dimers,<sup>5</sup> we assigned the two bands in the visible solution spectra of  $Rh_2(O_2CR)_4L_2$  to allowed  $\pi^* \rightarrow \sigma^*$  and  $\pi^* \rightarrow Rh-O \sigma^*$  transitions. The assignment was based on the close match between calculated and experimental energies, and the observed shifts in band energies with varying L. We have since completed explicit spin-polarized transition-state calculations of the excitation energies, which are compared with experiment in Table VI. Our assignment has recently received support from single-crystal polarized spectra of Rh<sub>2</sub>(O<sub>2</sub>CCH<sub>3</sub>)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub>.<sup>33,38</sup> The 1.7- and 2.3- $\mu$ m<sup>-1</sup> bands are found to be largely xy polarized, as predicted by the calculations. For each band a weaker z-polarized component appears at slightly lower energies than the xypolarized maximum. Since the  $\delta^*$  orbital lies just above the  $\pi^*$ orbital in our calculation, reasonable assignments for these zcomponents are forbidden  $\delta^* \rightarrow \sigma^*$   $(7b_{1u} \rightarrow 8b_{1u})$  and  $\delta^* \rightarrow Rh - O \sigma^* (7b_{1u} \rightarrow 5a_u)$  transitions, respectively, the intensity coming from a vibronic mechanism. Another reasonable possibility for the 2.3- $\mu$ m<sup>-1</sup> z component, which is the more prominent, is a  $\delta \rightarrow \sigma^* (9a_g \rightarrow 8b_{1u})$  transition. This excitation, uniquely among those below 3.0  $\mu$ m<sup>-1</sup>, is forbidden in D<sub>4h</sub>, but allowed in  $D_{2h}$  in the z direction.

The solution spectrum of  $Rh_2(O_2CCH_3)_4(H_2O)_2^+$  contains two bands completely analogous to those observed for the neutral species, but shifted to slightly higher energies.<sup>24,25</sup> This is in accord with the comparative orbital and excitation energies calculated for Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>(H<sub>2</sub>O)<sub>2</sub> and Rh<sub>2</sub>(O<sub>2</sub>CH)<sub>4</sub>- $(H_2O)_2^+$ , as shown in Figure 2 and Table VI. As a result of the upward energy shift, the band assigned to  $\pi^* \rightarrow Rh-O \sigma^*$ passes under the envelope of higher energy, higher intensity transitions in some solvents. The qualitative difference between the visible spectra of the cation and neutral species is the appearance of a new low-energy band near 1.3  $\mu$ m<sup>-1</sup> for the former. As indicated in Table VI, our calculations suggest a  $\delta \rightarrow \delta^*$  assignment for this band. We cannot entirely exclude an  $O \rightarrow \delta^*$  charge transfer assignment. The  $\delta \rightarrow \delta^*$  transition would be z polarized, and the  $O \rightarrow \delta^* xy$  polarized; thus single crystal polarized spectra could settle this question.

ESR Spectra of  $Ru_2(O_2CR)_4^+$  Complexes. The frozen-solution ESR spectrum of  $Ru_2(O_2CC_3H_7)_4Cl$  has been reported by Cotton and Pedersen.<sup>23</sup> Here we compare it with predictions from the present calculations. The discussion will be only qualitative, because of the large number of excited states which contribute, and because of significant experimental uncertainties in the spin Hamiltonian parameters. Nevertheless, we can show that the spectrum is at least consistent with the calculated electronic structure. The experimental spectrum can be analyzed in terms of a tetragonal spin Hamiltonian

$$H = \mu [g_{\parallel} H_z S_z + g_{\perp} (H_x S_x + H_y S_y)] + D[S_z^2 - S(S+1)/3] + E(S_x^2 - S_y^2) + A_{\parallel} S_z I_z + A_{\perp} (S_x I_x + S_y I_y)$$
(1)

where  $S = {}^{3}/{_{2}}$  and we consider the most likely mixture of Ru isotopes,<sup>23</sup> in which one nucleus is  ${}^{99}$ Ru or  ${}^{101}$ Ru, with  $I = {}^{5}/{_{2}}$ , and the other is  ${}^{96}$ Ru,  ${}^{98}$ Ru,  ${}^{100}$ Ru,  ${}^{102}$ Ru, or  ${}^{104}$ Ru, with I =0. The zero field splitting is sufficiently large (|2D| > 2.2cm<sup>-1</sup>) so that only the  $M_{s} = {}^{-1}/{_{2}} \rightarrow M_{s} = {}^{1}/{_{2}}$  transition is observed. Computer simulation of the 4.2 K spectrum yields the parameters  $g_{\perp} = 2.18$  and  $A_{\perp} = 3.1 \times 10^{-3}$  cm<sup>-1</sup>. Less precisely determined are  $g_{\parallel} = 2.1 \pm 0.1$  and  $|A_{\parallel}| = (9 \pm 3) \times 10^{-3}$  cm<sup>-1</sup>. The observed intensity pattern is inconsistent with a trapped-valence state in which the spin is localized at one of the ruthenium nuclei in the dimers.<sup>23</sup>

The theoretical expression for the g tensor, expanded through second order in perturbation theory, has the following general form:<sup>39</sup>

$$g_{zz} = 2 + \frac{1}{S} \sum_{n,p} \sum_{k} \frac{\langle \psi_p | l_k^z | \psi_n \rangle \langle \psi_n | \xi_k(r_k) l_k^z | \psi_p \rangle}{\epsilon_p - \epsilon_n}$$
(2)

Here  $\psi_p$  is any orbital that contains an odd electron,  $\psi_n$  is any orbital which is either full or empty, and  $\epsilon_p$  and  $\epsilon_n$  are the corresponding orbital energies. The sum over k is over all atoms in the molecule, with spin-orbit coupling constants  $\xi_k$ . In a crystal-field model, only the ruthenium nuclei would contribute. The orbital energy difference  $\epsilon_p - \epsilon_n$  may be replaced for greater accuracy by a transition-state estimate of the state energy difference. There are corresponding expressions for  $g_{xx}$  and  $g_{yy}$ .

The angular momentum operator transforms in  $D_{4h}$  as  $e_g$  $+ a_{2g}$ , so that symmetry considerations limit the number of excited states that need to be considered in eq 2. Consider, for example, the contributions to  $\Delta g_{\parallel}$ . In the crystal-field model, the only excited state that enters here is the promotion from the half-filled  $2b_{1u}$  (Ru-Ru  $\delta^*$ ) orbital to the  $4b_{2u}$  (Ru-O  $\sigma^*$ ) unoccupied orbital. This corresponds to an excitation from an orbital with  $d_{xy}$  character to one with character  $d_{x^2-y^2}$ , both orbitals having odd inversion symmetry. If this were the only excited state of importance, one would expect  $g_{\parallel} < 2$ , in line with the general rule that excited states formed by promoting an unpaired electron into an empty orbital give a negative contribution to the g-tensor element, reducing it from the free-spin value. The X $\alpha$ -SW calculation, however, shows two additional occupied orbitals of b<sub>2u</sub> symmetry that contain significant ruthenium  $d_{x^2-y^2}$  character: the  $2b_{2u}$  and  $3b_{2u}$  have 17 and 20% metal d character, respectively. Excitations from these orbitals into the  $2b_{1u}$  ( $\delta^*$ ) orbital will lead to positive g-tensor shifts. The observed value of g<sub>1</sub> will contain contributions from all three of these excited states.

We can follow common procedures<sup>40</sup> in an attempt to obtain a more quantitative estimate of these effects. We write the  $2b_{1u}$ ( $\delta^*$ ) molecular orbital in the form

$$|2b_{1u}\rangle = \frac{\alpha}{\sqrt{2}} (d_{xy}^{A} - d_{xy}^{B}) + \text{ligand contributions}$$
 (3)

where A and B label the ruthenium nuclei, and  $\alpha$  is an effective covalency parameter. In the muffin-tin model,  $\alpha^2$  gives the fraction of metal d character in this orbital.<sup>28</sup> In a similar fashion we write

$$|nb_{2u}\rangle = \frac{\beta_n}{\sqrt{2}} (d_{x^2-y^2} - d_{x^2-y^2} - d_{x^2-y^2})$$

+ ligand contributions (4)

where n = 2, 3, and 4. Values for  $\alpha$  and  $\beta_n$  are collected in

Table VII. Calculation of  $g_{\parallel}$  for  $Ru_2(O_2CH)_4Cl_2^-$ 

orbital	% Ru d character	6 <i>a</i>	$\Delta_n{}^b$	$\Delta g_{\parallel}{}^c$
2b1u	$0.71 \equiv \alpha^2$	-0.221		
$2b_{2u}$	$0.17 \equiv (\beta_2)^2$	-0.591	81 300	0.003
3b <sub>2u</sub>	$0.20 \equiv (\beta_3)^2$	-0.369	32 400	0.010
4b <sub>2u</sub>	$0.67 \equiv (\beta_4)^2$	-0.99	26 800	-0.042
			net	-0.029

<sup>*a*</sup> Orbital energy in hartrees. <sup>*b*</sup>  $\Delta_{\pi} \equiv \epsilon(2b_{1u}) - \epsilon(nb_{2u})$ , in cm<sup>-1</sup>. <sup>*c*</sup> Calculated from eq 6, assuming  $\lambda$  880 cm<sup>-1</sup>, a value between the atomic values for Ru<sup>0</sup> (878 cm<sup>-1</sup>) and Ru<sup>+</sup> (887 cm<sup>-1</sup>). The calculations predict ca. Ru<sup>0.4+</sup>.

Table VII, along with the corresponding orbital energies.

The matrix elements that appear in eq 2 can be evaluated by the approximate procedure suggested by Stone,<sup>39</sup> e.g.

$$\langle 2b_{1u} | l_A^Z + l_B^Z | 2b_{2u} \rangle \approx \frac{\alpha \beta_2}{2} \langle \mathbf{d}_{xy}^A | l_A^Z | \mathbf{d}_{x^2 - y^2} \rangle + \frac{\alpha \beta_2}{2} \langle \mathbf{d}_{xy}^B | l_B^Z | \mathbf{d}_{x^2 - y^2} \rangle = 2i\alpha \beta_2 \quad (5)$$

Proceeding in this fashion we find

$$g_{\parallel} = 2 + \frac{4\lambda\alpha^2}{S} \left\{ \frac{\beta_2^2}{\Delta_2} + \frac{\beta_3^2}{\Delta_3} - \frac{\beta_4^2}{\Delta_4} \right\}$$
(6)

where  $\Delta_n \equiv |\epsilon(2b_{1u}) - \epsilon(nb_{2u})|$  for  $n = 2, 3, 4, \text{ and } \lambda$  is the spin-orbit coupling constant for Ru, i.e., the integral of  $\xi(r)$  over the radial part of the d orbital. The three contributions to  $g_{\parallel}$  are also given in Table I. The net result is a small negative shift, which is probably within the experimental uncertainty of the small positive shift found in the computer simulation of the experimental spectrum.<sup>23</sup>

The calculation of  $g_{\perp}$  is still more complex because there are more excited states with the proper symmetry to contribute to the deviation from the free-spin value. The most important crystal-field-like excitation appears to be  $2b_{2g}(\delta) \rightarrow 6e_g(\pi^*)$ , which has a calculated excitation energy  $\Delta \simeq 8700$  cm<sup>-1</sup>. There is a also a lower lying 1b<sub>2g</sub> orbital with significant Ru d character that would also contribute. A second set of contributions comes from  $5e_u$ ,  $6e_u$ ,  $7e_u$  (all  $\pi$  character) $\rightarrow 2b_{1u}(\delta^*)$ . Yet another set is  $5a_{1g}$ ,  $6a_{1g}$ ,  $7a_{1g}$  (d<sub>z2</sub> or  $\sigma$ -bonding character) $\rightarrow 6e_g(\pi^*)$ . All of these correspond to excitations into a partially filled orbital, and hence lead to positive g-tensor shifts. The only crystal-field-like excitation that can lead to a negative shift is  $6e_g(\pi^*) \rightarrow 5b_{1g}(Ru - O\sigma^*)$ , and this will be balanced in part by the promotion  $4b_{1g} \rightarrow 6e_g$ with a positive shift. Thus the observed positive g-tensor shift is completely consistent with the electronic structure proposed here. If we adopt the approximations listed above for  $g_{\parallel}$ , the ten excited states listed here combine to give  $g_{\perp} = 2.18$ , in excellent agreement with the observed value.23

It may be prudent at this point to list some of the uncertainties in the present calculation, in order to indicate why such results should be viewed as semiquantitative at best. Aside from intrinsic inaccuracies in the  $X\alpha$ -SW model, there are at least three additional possible sources of error. (1) State energy differences may not be well approximated by orbital energy differences. While in the present case this could be improved by transition-state calculations, such results are unlikely to have an absolute accuracy better than about 4000 cm<sup>-1</sup>, and uncertainties of this magnitude can be important in a quantitative calculation. (2) Our treatment of covalency effects has been quite crude. A more correct version would recognize that covalency affects the spin-orbit and orbital Zeeman matrix elements of eq 2 in different ways.<sup>28,41</sup> Further, the use of a single spin-orbit coupling constant to represent all orbitals is a serious limitation.<sup>28,41-43</sup> While it is feasible in the scattered-wave model to handle covalency in a more correct fashion,<sup>28</sup> not all of the error can be removed; in view of the additional experimental and theoretical uncertainties for the present case, such calculations do not seem warranted. (3) Contributions to the g tensor in third order in perturbation theory will arise from doublets as well as quartet states.<sup>44</sup> Since some of these may have excitation energies below those of the quartet states considered above, it is not clear that third-order contributions may safely be ignored.

It is worth noting that these difficulties are not unique to a molecular orbital or  $X\alpha$  approach, but must be faced even by possibly more accurate ab initio calculations.<sup>45</sup> It does not seem likely that any current method could quantitatively predict the behavior of systems as large as this one in an a priori fashion.

We consider next the hyperfine structure due to the ruthenium nuclear spin, and organize our discussion around the various terms that enter in perturbation theory. Two terms enter in first order. One is the Fermi contact term, related to the spin density at the ruthenium nucleus. In the spin restricted theory this term vanishes, because the unpaired electrons are in d-like molecular orbitals. Spin polarization effects can lead to a finite spin density at the nucleus. In the present spin unrestricted calculation

$$\rho^{\rm spin}(0) \equiv \sum_{\alpha} \psi_i^{\ 2}(0) - \sum_{\beta} \psi_i^{\ 2}(0) = -0.403 a_0^{-3}$$
(7)

This corresponds to a hyperfine coupling constant for  $^{99}$ Ru of

$$a_{\rm Ru} = \left(\frac{4\pi}{3M_{\rm s}}\right) g_{\rm e}\beta_{\rm e}g_{\rm N}\beta_{\rm N}\rho^{\rm spin}(0) \simeq 9 \times 10^{-4} \,\rm cm^{-1} \quad (8)$$

We have no good way of estimating the probable error in this number. X $\alpha$  calculations on first-row transition-metal complexes show that this sort of calculation often underestimates the extent of s-orbital polarization.<sup>28,46</sup> Comparable studies are not available for heavier elements, but it seems likely that the estimate in eq 7 and 8 is also an underestimate, perhaps by 100% or more.

A dipolar term also contributes in first order, with the perturbation expression

$$A_{xx}^{\circ} = \frac{g_e \beta_e g_N \beta_N}{M_s} \sum_i \left( \frac{3(r_x^i)^2 - (r^i)^2}{(r^i)^5} \hat{S}_z^i \right)$$
(9)

where  $r^i$  is the position of the *i*th electron and  $S_z^i$  is the z component of its spin operator. In the present case the spin distribution around each Ru nucleus is the sum of  $d_{xy}$ ,  $d_{xz}$ , and  $d_{yz}$ -like orbitals, the net spin distribution being nearly spherically symmetric. This leads to very small first-order dipolar contributions for both the spin-restricted and unrestricted calculations,  $A_{\parallel}^{\circ} = -2A_{\perp}^{\circ} \simeq -0.6 \times 10^{-4} \text{ cm}^{-1}$ .

Second-order contributions to the hyperfine tensor can conveniently be divided into three parts.<sup>47</sup> The first involves an interaction between the orbital moment of the electron and the nuclear magnetic moment, which leads to a contribution proportional to the deviation of the g tensor from its spin-only value; e.g.

$$\Lambda_{\perp}' = g_{\rm e}\beta_{\rm e}g_{\rm N}\beta_{\rm N} \langle r^{-3} \rangle (g_{\perp} - 2) \tag{10}$$

As with the g tensor, only excited states of the same multiplicity as the ground state contribute. The notation  $\Lambda'$  follows Maki and McGarvey,<sup>48</sup> and  $\langle r^{-3} \rangle$  is a radial expectation value of the inverse cube of the distance of the electron in an unpaired orbital from one of the Ru nuclei. For the metal-metal dimer case, this should be roughly half the value of a ruthenium 4d atomic orbital, which is about  $6a_0^{-3}$ . With this estimate  $\Lambda_{p'}$  is  $\sim -4 \times 10^{-4}$  cm<sup>-1</sup>. Since this is an order of magnitude smaller than the observed hyperfine tensors, it is clear that a more precise estimate is not of qualitative significance.

Other second-order terms arise from the interaction of the nuclear magnetic moment with the spin moment of the electron.<sup>40</sup> Contributions of this sort from excited quartet states are similar in magnitude to the tensor  $\Lambda'$  discussed above, and cannot be used to rationalize in a simple way the qualitative hyperfine behavior. Doublet states of the form  $(\pi_x^*)^2(\delta^*)$  or  $(\pi_v^*)^2(\delta^*)$  can mix with the ground state via spin-orbit coupling, but these states do not contribute in second order since matrix elements of the form (ground state|hyperfine perturbation excited doublet vanish. Such states, because of their low excitation energies, may be important in higher orders of perturbation theory. Because dozens of terms would enter, such a calculation does not seem warranted given our present level of theoretical uncertainties.

From this qualitative discussion we can conclude that the "common" first- and second-order hyperfine effects are small for  $Ru_2(O_2CH_2)_4^+$  and that the observed coupling appears to arise from a large number of second-order terms or from higher order effects. For this and similar systems, then, it will be difficult to extract detailed bonding information from the ESR spectra.

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Supplementary Material Available: Table I, sphere radii and SCF charge distributions (1 page). Ordering information is given on any current masthead page.

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